

Examination questions (second exam)

7.10.2015

Mathematical Cryptology MAT-63256

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Examination date:

Instructions:

Use of books, notes, dictionaries, ebooks, calculators and computers allowed.

Questions:

1. Assume that the letters a,b,c,d,e,f,g are encoded as the integers 0,1,2,3,4,5,6 mod 7, in that order. Encrypt the following plaintext into ciphertext words using the affine encryption $4i+4$:

deaf babe gab, feed a cab

2. Find all irreducible (prime) polynomials of degree 3 over a 2-element field.

3. What are the decrypting functions for the AFFINE encryption $4i+3 \pmod{7}$ and $\pmod{11}$?

4. Which elements of the multiplicative group of the 7-element field $F(7)$ of residues mod 7 have order 3 ?

5. How many affine encrypting keys exist mod 13 ?